

# Tensor-Directed Simulation of Strokes for Image Stylization with Hatching and Contours



**David Tschumperlé**

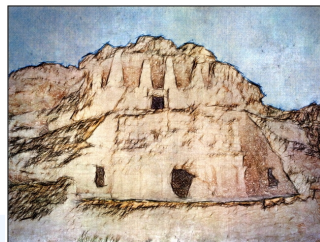
Image Team, GREYC / CNRS (UMR 6072)

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- **Context** : **Non-Photorealistic Rendering** (NPR).
- **Motivation** : Render a photograph as a **sketch** or a pencil drawing.
- **Method** : **B&W stroke-based algorithm**. Place (black) graphic primitives on an white canvas, according to the **geometry of the initial image**. Then, colorize the result.



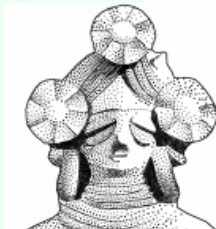
Original color image



Final rendering



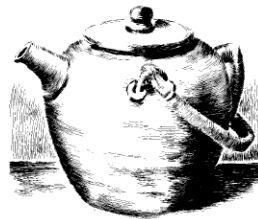
# Overview : State of the art of B&W NPR



Deussen-Hiller-etal  
(*stipple drawing*)



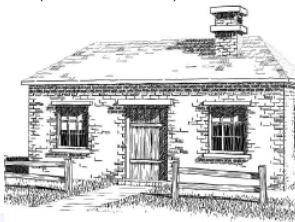
Durand-Ostromoukhov-etal  
(*interactive method*)



Salisbury-Wong-etal  
(*oriented textures*)



Hertzmann-Zorin  
(*from 3d models*)



Winkenbach-Salesin  
(*from 3d models*)



Salisbury-Anderson-etal  
(*interactive method*)

We propose (yet) another **stroke-based algorithm** with :

- Straight or curved **lines** as graphic primitives.
- 2<sup>nd</sup>-order **tensors** for analyzing the local image geometry **and** modeling the pencil paths.
- Ability to render image **contours** and **hatching** within **the same single process**.
- Use the **flexibility** of the tensor model to allow **multiple drawing styles** with the same algorithm and from the same input image.

⇒ Try to simulate pencil strokes as they would be drawn by an artist !

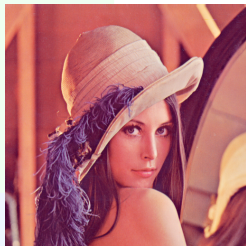
# Illustration of the proposed method



Same input image leads to multiple styles of pencil rendering

# A first naive approach

- 1 Compute the image luminance  $Y : \Omega \rightarrow \mathbb{R}$ , and its smoothed gradient  $\nabla Y_\sigma = \nabla Y * G_\sigma$ .
- 2 Create an empty (white) canvas  $S : \Omega \rightarrow \mathbb{R}$ .
- 3 Repeat  $N$  times :
  - 1 Pick one random position  $\mathbf{X} = (x, y)$  in  $\Omega$ .
  - 2 Draw a semi-transparent straight line  $\mathbf{X} - L_{\xi(\mathbf{x})} \rightarrow \mathbf{X} + L_{\xi(\mathbf{x})}$  on  $S$ ,  
where  $\xi(\mathbf{x}) = \frac{\nabla Y_{\sigma}^\perp(\mathbf{x})}{\|\nabla Y_{\sigma}(\mathbf{x})\|}$  (contour direction at  $\mathbf{X}$ ).



Color image  $I$

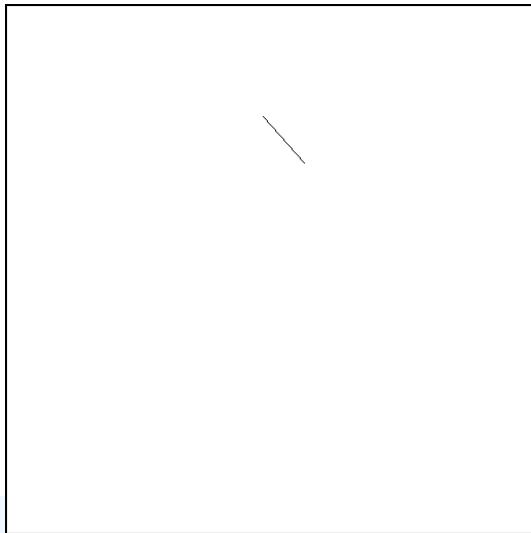


Luminance  $Y$



Smoothed gradient  $\nabla Y_\sigma$

# After 1st iteration



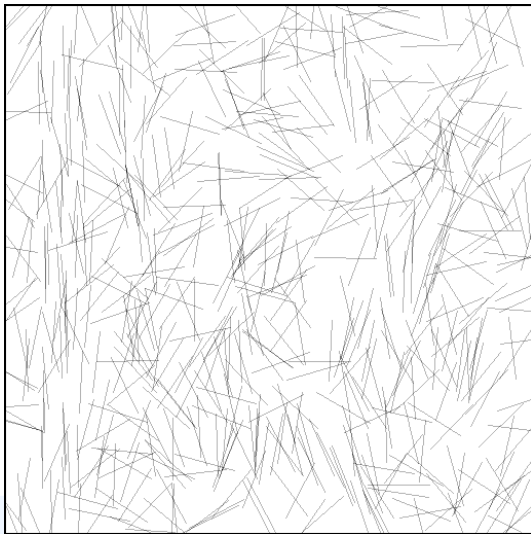
Canvas **S**

# After 200th iterations



Canvas **S**

# After 600th iterations



Canvas **S**

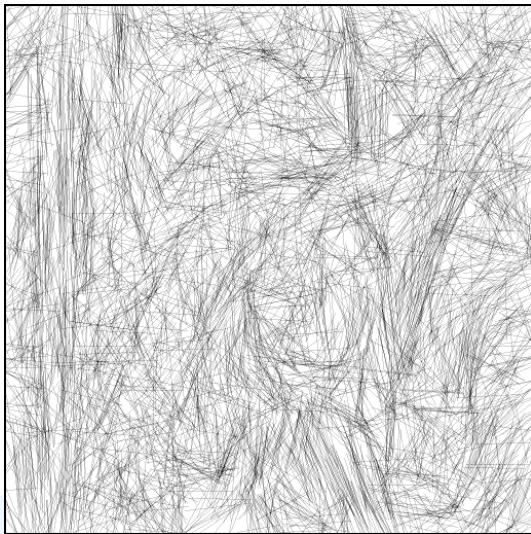
# After 1200th iterations



Canvas **S**

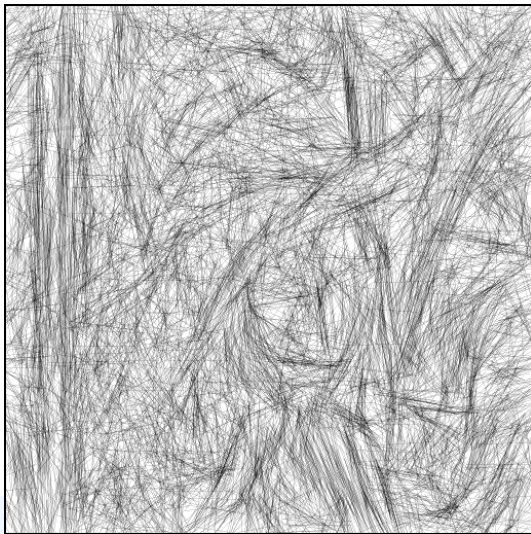


# After 4800th iterations



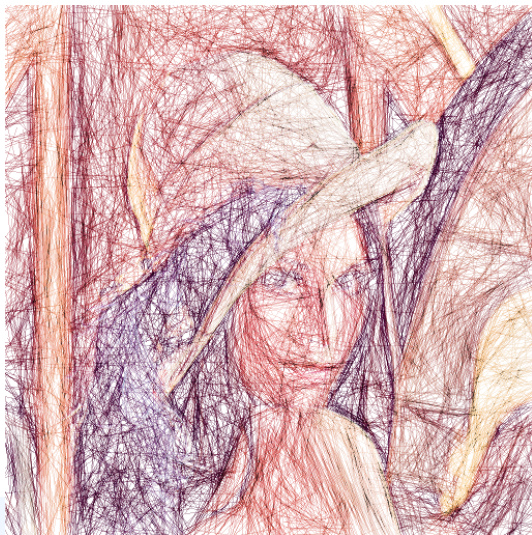
Canvas **S**

# After 10000th iterations



Canvas **S**

# After 10000th iterations (colorized)



Canvas **S** + Colorization

# Edge-focused modification

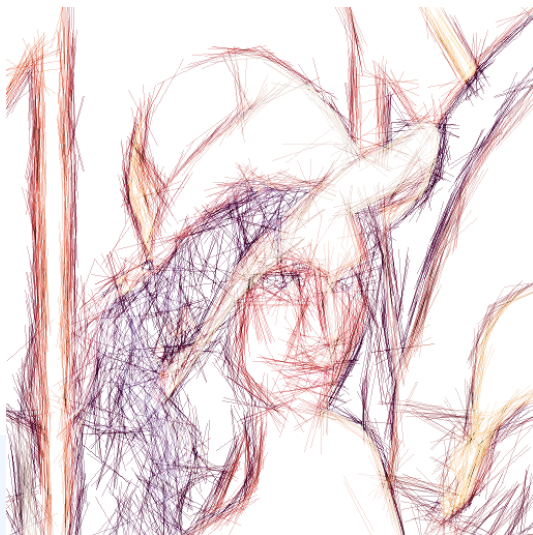
- Draw a pencil stroke at **X** only when  $\|\nabla Y_{\sigma}(\mathbf{x})\| > \epsilon$  (i.e. **X** is on a significant edge).



# Edge-focused modification (colorized)



- Draw a pencil stroke at **X** only when  $\|\nabla Y_{\sigma}(\mathbf{x})\| > \epsilon$  (i.e. **X** is on a significant edge).



- 1 Only **straight** lines.
- 2 **Poor analysis** of the image **geometry** (simple gradient, no analysis of the color variations).
- 3 **No spatial coherence** (or no drawing) on flat image regions.



⇒ **Can be easily improved by considering tensor models !**

- Inspired by the formalism of **diffusion tensors**, used for directing **PDE-based anisotropic smoothing processes**.

[Weickert:98, Tschumperle-Deriche:03,...]

$$\frac{\partial I}{\partial t} = \text{div}(\mathbf{D} \nabla I) \quad \text{or} \quad \frac{\partial I}{\partial t} = \text{trace}(\mathbf{D} \mathbf{H})$$

- Based on the **analysis of the local image geometry** through the computation of the **structure tensor** [DiZenko:86].

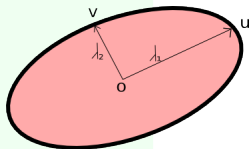
$$\mathbf{G}_{\alpha, \sigma} = \left( \sum_i \nabla \mathbf{I}_{i\alpha} \nabla \mathbf{I}_{i\alpha}^T \right) * G_{\sigma}$$

- Eigenvalues/eigenvectors of  $\mathbf{G}_{\alpha, \sigma}$  are **robust local geometric estimators** of the image structures. Diffusion tensors  $\mathbf{D}$  are built upon  $\mathbf{G}_{\alpha, \sigma}$  and direct the smoothing process  
→ *Anisotropic diffusion*.

# From diffusion tensors (illustrated)...

$$T = \lambda_1 \mathbf{u}\mathbf{u}^T + \lambda_2 \mathbf{v}\mathbf{v}^T$$

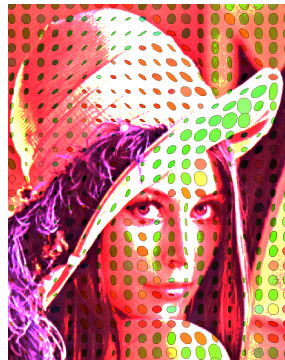
$$= \begin{pmatrix} a & b \\ b & c \end{pmatrix}$$



2nd order tensor  $\mathbf{T}$



Structure tensors field  $\mathbf{G}_\sigma$



Diffusion tensors field  $\mathbf{D}$

⇒ Diffusion tensors model the way a digital painter would apply the “smudge tool” to smooth the noise and remove image artefacts.



- **Structure tensors** are able to locally distinct between **different types of image regions** :

- 1 **Flat regions** : Small isotropic tensors.
- 2 **Contours** : Anisotropic tensors, oriented  $\perp$  to the contour.
- 3 **Small-scale texture** : Large isotropic tensors.

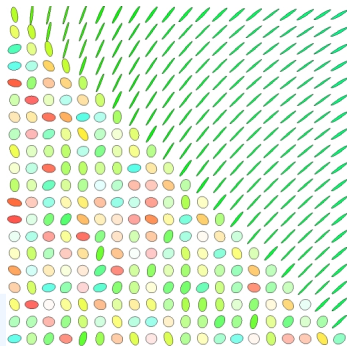
- From an “**sketching**” **point of view**, this would correspond to different **drawing behaviors** :

- 1 **Flat regions or textures** : Regular strokes forming a **coherent hatching pattern**.
- 2 **Contours** : **Oriented strokes**, along the contour direction.

⇒ **Strokes geometry can be successfully modeled by a tensor field  $T$  that depends on  $G_{(\alpha, \sigma)}$  !**

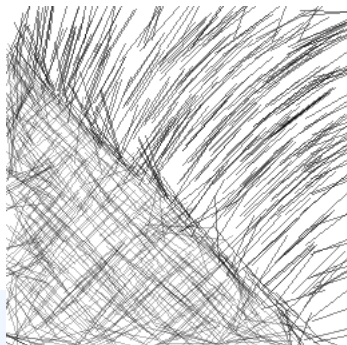
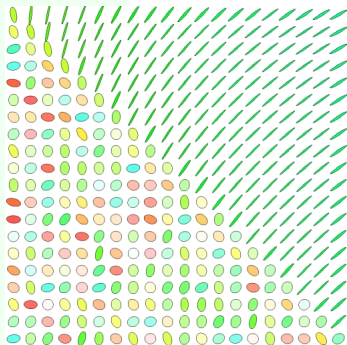
[See paper content for more details about our proposal]

- From an “sketching” point of view, this would correspond to different **drawing behaviors** :
  - Flat regions or textures** : Regular strokes forming a **coherent hatching pattern**.
  - Contours** : **Oriented strokes**, along the contour direction.



⇒ **Stroke tensors variability will lead to different drawing styles.**

- **Question** : How to draw strokes on canvas  $S$  with respect to the stroke tensor field  $\mathbf{T}$ , such that :
  - 1 Small isotropic tensors locally render **very few strokes**.
  - 2 Large isotropic tensors locally render **hatches**.
  - 3 Anisotropic tensors locally render **oriented contour strokes**.



- **Stroke throwing algorithm** : Initialize an empty canvas  $S$  and compute the stroke tensors  $T$  from the input image  $I$ .

For each angle  $\gamma$  from a given set  $[\gamma_0, \gamma_1, \dots, \gamma_N]$ , do :

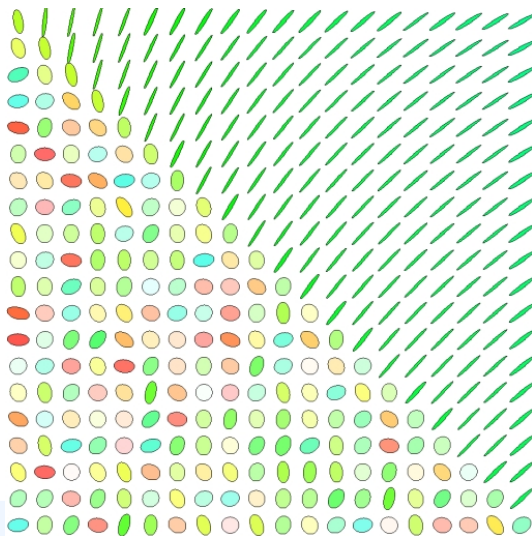
- 1 Compute vector field  $w_\gamma = \sqrt{T} a_\gamma$  with  $a_\gamma = (\cos \gamma \ \sin \gamma)^T$ .
  - 2 Repeat  $N$  times :
    - 1 Pick one random position  $X = (x, y)$  in  $\Omega$ .
    - 2 Draw a semi-transparent straight line  $X - L\xi_{(X)} \rightarrow X + L\xi_{(X)}$  or a streamline of  $w_\gamma$  starting from  $X$  and of length  $L$ , on  $S$ .
- The stroke tensors are used to **distort** each direction  $a_\gamma$ , according to the geometry of the input image.
  - The chosen number of angles  $\gamma$  set **the style of the hatches**.
  - **Streamlines** allow drawn strokes to be **curved**.

# Illustration of the algorithm



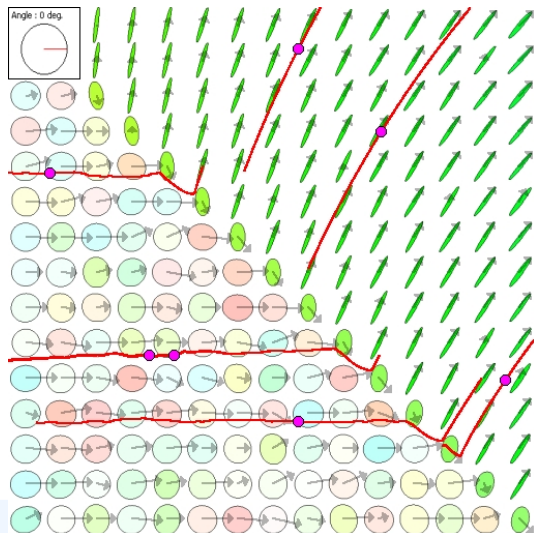
Input image (synthetic).

# Illustration of the algorithm



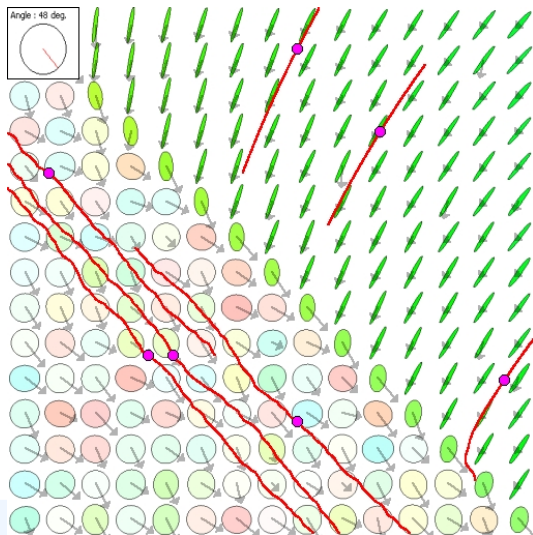
Computed field of stroke tensors.

# Illustration of the algorithm



Some streamline strokes drawn for  $\gamma = 0^\circ$ .

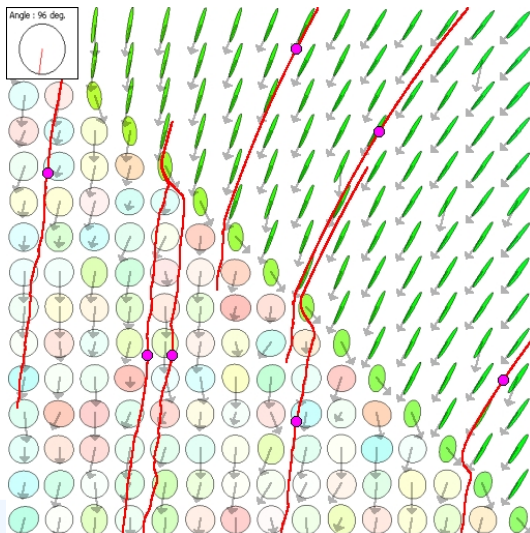
# Illustration of the algorithm



Some streamline strokes drawn for  $\gamma = 48^\circ$ .

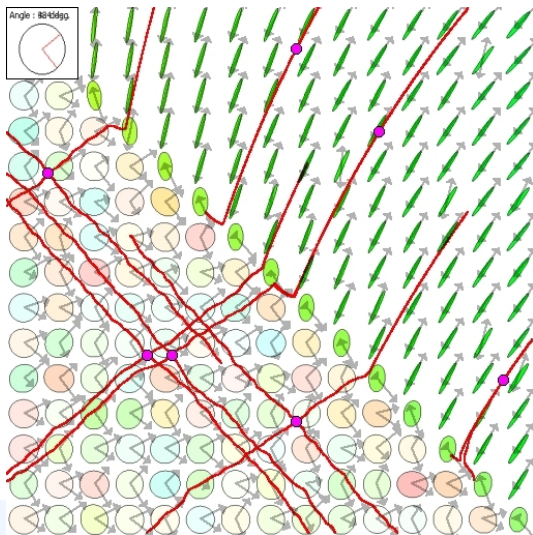


# Illustration of the algorithm



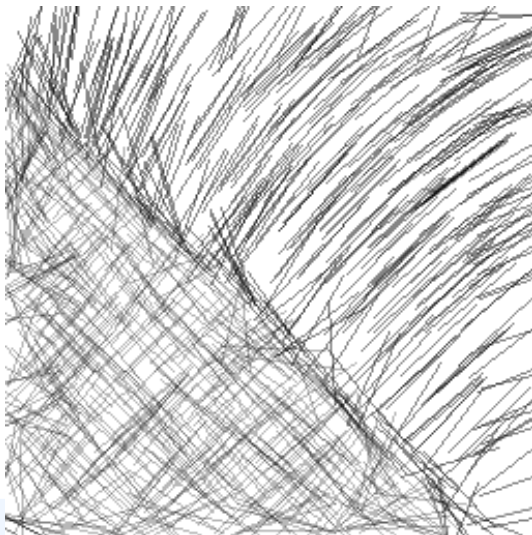
Some streamline strokes drawn for  $\gamma = 96^\circ$ .

# Illustration of the algorithm



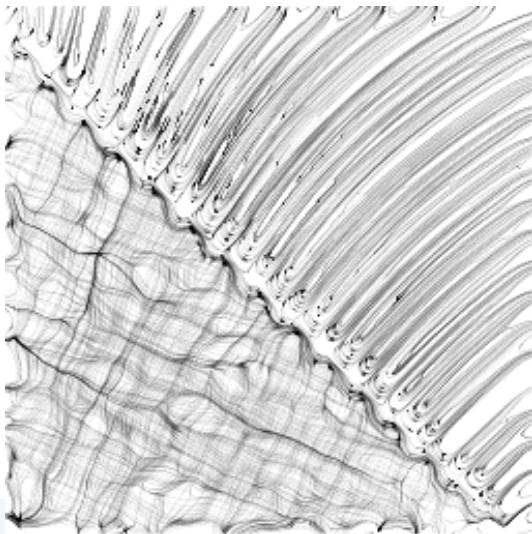
Some streamline strokes drawn for  $\gamma = 45^\circ$  and  $\gamma = 135^\circ$ .

# Illustration of the algorithm



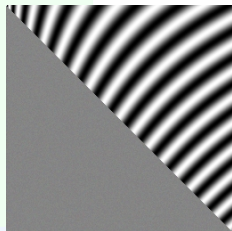
Final result with straight lines,  $\gamma = 45^\circ$  and  $\gamma = 135^\circ$ .

# Illustration of the algorithm

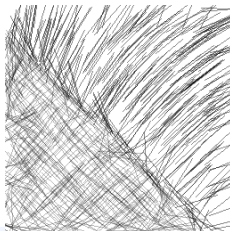


Final result with curved lines,  $\gamma = 45^\circ$  and  $\gamma = 135^\circ$ .

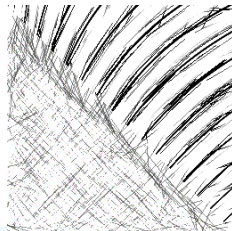
- Colorization combines the B&W sketch canvas and the colors of the input image, **to add colors to the generated sketch**.
- Here, we tried very simple combinations only, also known as **layer blending modes** : **Soft light, hard light, overlay,....**
- All results shown afterwards are using these simple coloring techniques.



Input image

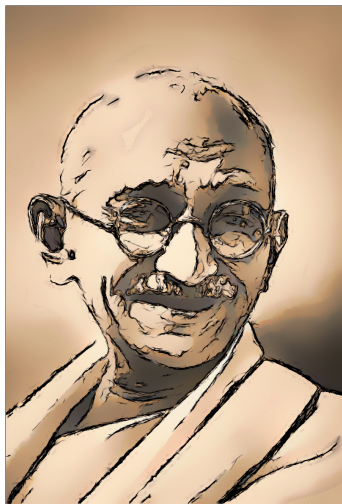
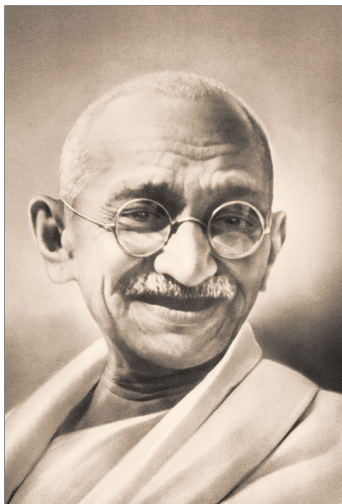


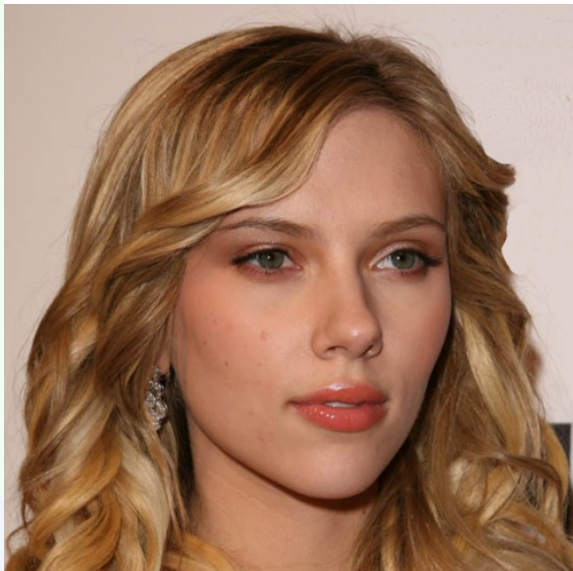
B&W sketch

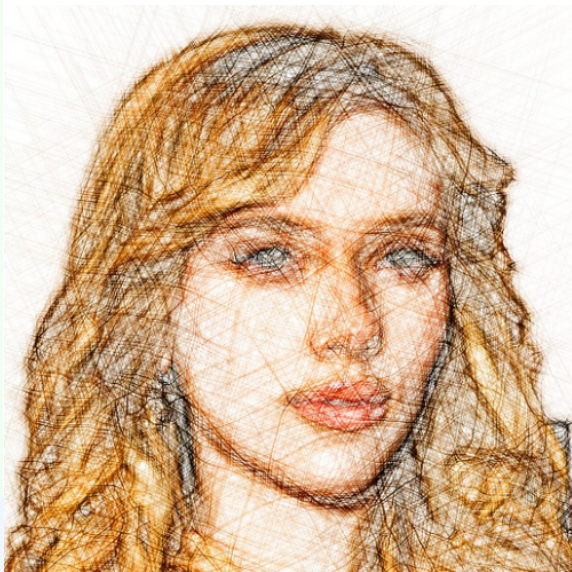


"Colorized" result

- Some straightforward applications of the sketch algorithm, with simple colorization steps...









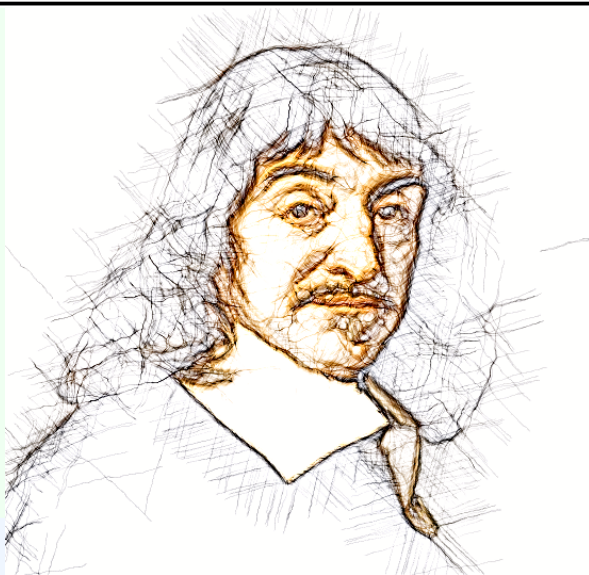
- Can be used to simulate **several different drawing steps** towards a final painting.



Step 1 (straight strokes)



Step 2 (curved strokes)



Step 3 (curved strokes + colorization)



Step 4 (curved strokes + colorization)



Final painting (the only input image of the algorithm !)



(Colors do not have to match the input image)

- Several sketch results can be also merged together to render even more complex rendering (courtesy of **Tom Keil**).



- Several sketch results can be also merged together to render even more complex rendering (courtesy of **Tom Keil**).















## ● **Conclusions :**

We have proposed a B&W stroke-based algorithm for simulating the drawing of lines, to convert photographs into sketches.

- ① It uses **tensor fields** to deal with the geometry both of the **image** and the **strokes**.
- ② It defines a way to draw strokes **according to the geometric shape of the tensor field**.

## ● **Perspectives :**

- ① Find the best ways to model the stroke tensors according to a **given artistic style**.
- ② Improve the **colorization step**.
- ③ Model the **thickness** of strokes.
- ④ Deal with **image sequences** (temporal coherence).

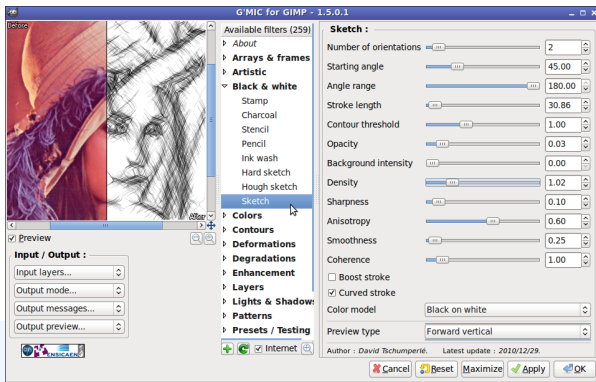


# Do it yourself !

- The algorithm code is available in **G'MIC**, a powerful framework for image processing, developed at the **GREYC/Image** lab.

<http://gmic.sourceforge.net>

- Try our sketch algorithm, with the **G'MIC** plug-in for **GIMP**.



# Questions ?



(Don't shoot the speaker !)